York University

Lassonde School of Engineering EECS

MATH 1090A. Problem Set #4 Posted November 18, 2016

Due: December 5, 2016; 3:00pm, in the course box

Annotation is required!

(5 MARKS/Each) Do the following problems.

1. Correctly state and prove the bound variable renaming metatheorem for \exists .

An Equational proof is required.

2. True or False? $(\exists \mathbf{x})(A \to B) \vdash (\exists \mathbf{x})A \to (\exists \mathbf{x})B$.

If you answered "True", then give a proof.

If you answered "False", then give a semantic proof (countermodel) of your claim.

3. True or False?

$$\vdash \Big((\forall \mathbf{x}) A \to (\forall \mathbf{x}) B \Big) \to (\forall \mathbf{x}) (A \to B)$$

If you answered "True", then give a proof.

If you answered "False", then give a semantic proof (countermodel) of your claim.

From the Text:

- **4. Section 6.6:** Numbers 2, 18, 19, 23, 24, 32
- **5. Section 8.3:** Numbers 8, 10, 11

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