## COSC 4111/5111 — Winter 2014

Posted: Jan 17, 2014
Due: TBA by a NEWS item on the course web page.

## Problem Set No. 1

NB. All problems are equally weighted and will be assigned a letter grade; an overall letter grade for the paper will be computed using York's 0-9 gpa scale.

The problem set list for grad students enrolled in CSE5111 is the entire list here. Undergrads should omit the problems marked "Grad".

This is not a course on formal recursion theory. Your proofs should be informal (but NOT sloppy), completely argued, correct, and informative (and if possible short). Please do not trade length for correctness or readability.

All problems are from the "Theory of Computation Text", or are improvesations that I completely articulate here.
(1) Dress up the primitive recursion

$$
\begin{aligned}
& \operatorname{two}(0)=1 \\
& \operatorname{two}(x+1)=\operatorname{two}(x)+\operatorname{two}(x)
\end{aligned}
$$

to make it conform with the rigid primitive recursion schema.
(2) (Grad). Do Exercise 2.1.2.43

## From Section 2.12.

(3) (Grad). Do problems 4, 20, 22.
(4) Do problems 6, 11, 12, 19.
(5) Write a "nice and clean" loop program which computes $\lambda x .\lfloor x / 2\rfloor$. The program must only allow instruction-types $X \leftarrow 0, X \leftarrow X+1, X \leftarrow Y$ and Loop $X \ldots$...end. It must not nest the Loop-end instruction! It is required that you give a convincing general argument (not a "trace") as to why your program works as specified.
(6) Do problem 27, 28.
(7) (Grad). Do problem 24, 29.

