### EECS 4422/5323 Computer Vision Feature Detection Lecture 3

Calden Wloka

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Calden Wloka (York University)

Image Representation

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### Announcments

- Bring your Python questions to office hours or labs
  - Recommendation for your own machine: Anaconda
  - Installing OpenCV through conda: link
  - Note that matplotlib works differently in Jupyter than in standard Python, requires matplotlib.pyplot.show() to display figure windows

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### Outline

- Linking Edge Elements
- Parametric Fitting
- Contour Voting
- Gestalt Principles

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- For many applications, it is better to have a localized edge line rather than a gradient map
- One way to better localize edges is through a Laplacian
- The individual localized points responding to the Laplacian are *edge elements*
- Let's demo the behaviour of a Laplacian filter...

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- 3. Apply non-maximum suppression along the gradient
- 4. Double-threshold employ hysteresis when eliminating weak edges

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### Hysteresis

*Hysteresis* is the dependence of a system's state on its past. It is applied in this case to the retention of edges with strength below the first higher threshold but above the second threshold (*weak edges*).

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Let's look at a Canny demo.

### Contours

Even with more strongly localized edges, we are still essentially left with a map of disparate edge elements. To begin reasoning over them or characterizing their properties, we need to form relationships between the edge elements to form larger cohesive structures.

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Contours are formed by taking edge elements and grouping them, usually through connected components with added rules. We can see an example with OpenCV's findContours() function.

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Once we have a set of contours, we can begin to work directly with them to reason over the content of the image or infer useful information, for example:

• Compute bounding boxes over objects with closed contours

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- Compute bounding boxes over objects with closed contours
- Encode additional logical steps to manipulate contours based on whole contour attributes, rather than kernel neighbourhoods
  - Link contour segments even across gaps
  - Eliminate isolated or topologically unsatisfying contour segments

### Parametric Segments

Often it is preferable to take another abstraction step over contour segments and fit a parametric curve rather than model it explicitly as a set of linked edge elements.

• More compact representations

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### Parametric Segments

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- More compact representations
- Allows straightforward applications of algebraic operations (*e.g.* calculate intersections)
- Can sometimes eliminate small quantities of noise

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### **Piecewise Linear Fitting**

Approximating a curve with an increasing number of small linear segments (each increase is done by finding points on the curve furthest from the current approximation).



### **Splines**

Instead of piece-wise linear approximations, we can instead utilize piecewise polynomial fitting (splines).

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- Random sample consensus (RANSAC)
- Hough Transform

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### RANSAC

### The Challenge of Outliers

When trying to link up disparate contour segments, we often face the challenge of spurious segments (either because they more properly belong to another grouping, or because they are an edge element based on noise).





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### RANSAC

### Random Sampling

RANSAC runs a number of trials, each time sampling a minimal set of data to fit a parametric model (such as a line).



Image source: Modified from Wikipedia

## Sample Voting

For each random sample, the fitted model is tested to see how much of the data it explains.



Image source: Modified from Wikipedia

### Fit Selection

The fit which best explains the majority of data is accepted. Only data which is consistent with this fit (within an allowable error threshold) is considered part of the final fit; all other data is considered an outlier.





### Fair Voting

One drawback to RANSAC is that it is stochastic, and only guaranteed to provide a good solution with a certain probability based on the number of random sample steps taken. A deterministic alternative is the *Hough transform*.

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If gradient information is retained to assign an orientation to a given edge element, then voting can be restricted to elements in accumulator space which are consistent with a given orientation. Without orientation, edge elements typically vote for all possible oriented lines passing through them, leading to a significant increase in computational requirements.

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### Accumulator Space

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Image source: Original source unknown

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- For lines, this is typically implemented in  $\rho$ - $\theta$  coordinates
- Accumulator space can be very large for pixel-wise accuracy
- Often accumulator space is implemented over a coarse spatial scale, and then fit is refined



Image source: Original source unknown

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### Hough Transforms for All

Although originally developed for line detection, Hough transforms can be readily adapted to arbitrary parametric shapes, and are particularly popular for circles and ellipses.



Image source: Peng, 2010

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Although originally developed for line detection, Hough transforms can be readily adapted to arbitrary parametric shapes, and are particularly popular for circles and ellipses.



What changes about the accumulator space for a circle transform instead of a line?

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Hough Transform

### Hough Transforms Example

Go to Hough Transform example.

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### Useful Tool for Constrained Applications

If you know what sorts of curves and lines you should find in an image, these tools can be very straightforward to implement and execute while still achieving satisfactory results. Examples of applications for which these would be well suited include, especially for situations with minimal training data:

Scanned form analysis

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If you know what sorts of curves and lines you should find in an image, these tools can be very straightforward to implement and execute while still achieving satisfactory results. Examples of applications for which these would be well suited include, especially for situations with minimal training data:

- Scanned form analysis
- Counting repetitive objects

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### Useful Tool for Constrained Applications

If you know what sorts of curves and lines you should find in an image, these tools can be very straightforward to implement and execute while still achieving satisfactory results. Examples of applications for which these would be well suited include, especially for situations with minimal training data:

- Scanned form analysis
- Counting repetitive objects
- Detecting reliable structures (field lines in sports, windows or building contours)

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### **Overarching Principles**

The heuristics and rules we have covered so far for how to select and group contours and fit lines and curves to those contours are drawn from a set of psychological principles known as *Gestalt Principles* (or *Gestalt Laws* or *principles of grouping*).

These general rules do not fit all possible situations in visual perception, but they do give us a nice starting point when reasoning over lines, curves, and contours (or even other features, like patches).

### Proximity

 Items which are close by tend to be interpreted as forming a group

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### Proximity

- Items which are close by tend to be interpreted as forming a group
- Items can be grouped by spatial proximity even if highly different in appearance (some caveats see *similarity*)

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### Proximity

- Items which are close by tend to be interpreted as forming a group
- Items can be grouped by spatial proximity even if highly different in appearance (some caveats see *similarity*)
- Grouped elements can create the illusion of shapes, even when not touching

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### Similarity

 Items which are similar in appearance are more likely to be grouped together than objects which are different in appearance



Image source:Wikipedia

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### Similarity

- Items which are similar in appearance are more likely to be grouped together than objects which are different in appearance
- Can work in tandem or be in conflict with *proximity*

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Image source:Wikipedia

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### Similarity

- Items which are similar in appearance are more likely to be grouped together than objects which are different in appearance
- Can work in tandem or be in conflict with *proximity*
- Can operate along disparate feature channels (*e.g.* colour, texture, shape)

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Image source:Wikipedia

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### Closure

 Despite gaps, we tend to group edges into complete, closed contours



Image source:Wikipedia

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### Closure

- Despite gaps, we tend to group edges into complete, closed contours
- Heavily informed by border ownership, which will be discussed later



Image source:Wikipedia

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### Closure

- Despite gaps, we tend to group edges into complete, closed contours
- Heavily informed by *border* ownership, which will be discussed later
- Influenced by surrounding context, semantic knowledge, strength of existing edges, and size of the gaps





### Continuation

 Perceptual preference is given to items being uninterrupted, cohesive objects



Image source:Wikipedia

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### Continuation

- Perceptual preference is given to items being uninterrupted, cohesive objects
- Curves and lines tend to follow an established direction, rather than sharp or abrupt changes



Image source:Wikipedia

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### Continuation

- Perceptual preference is given to items being uninterrupted, cohesive objects
- Curves and lines tend to follow an established direction, rather than sharp or abrupt changes
- When abrupt changes do occur, they tend to indicate occlusions or boundaries



Image source:Wikipedia

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