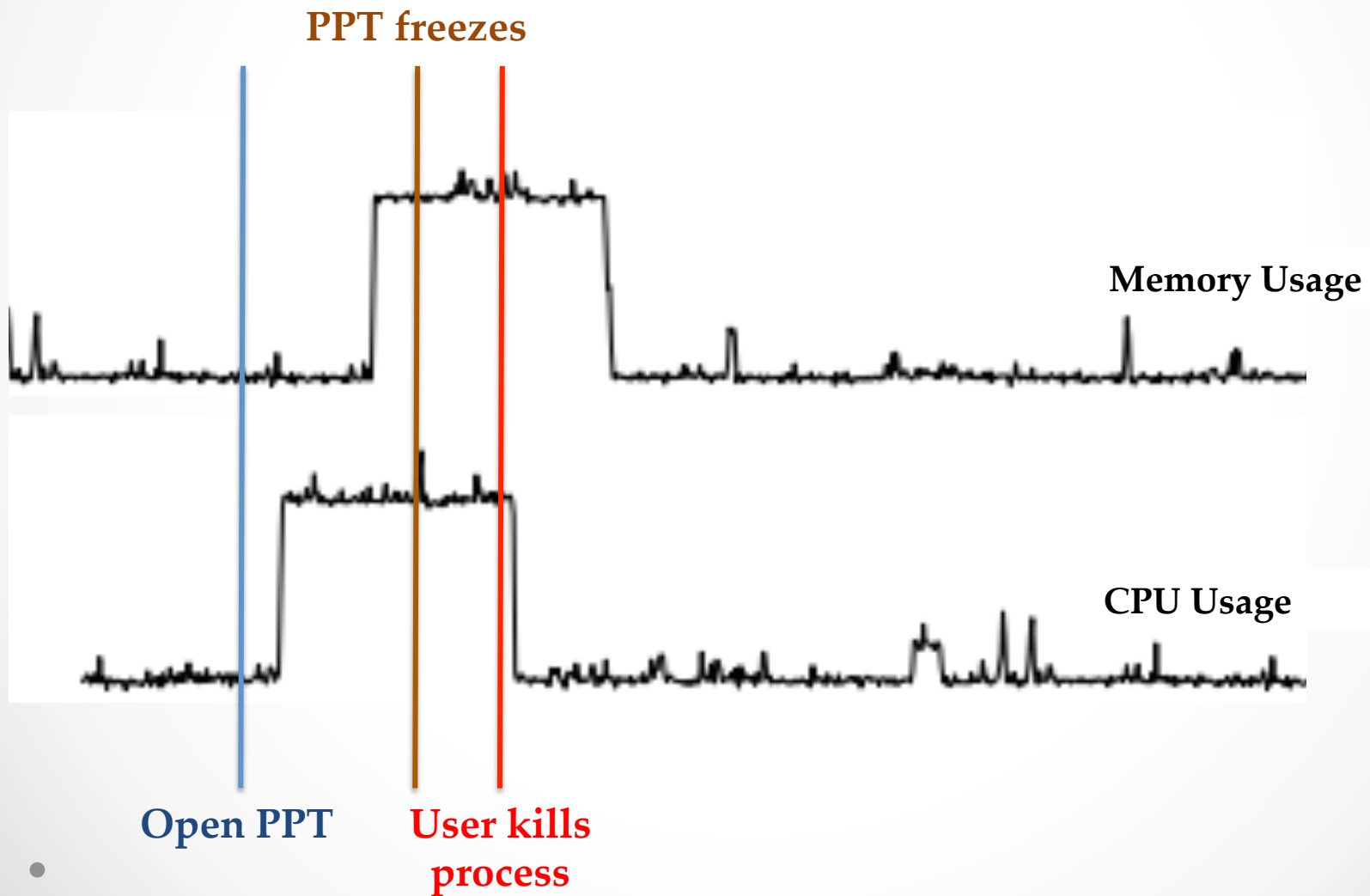


# Correlating Events with Time Series for Incident Diagnosis

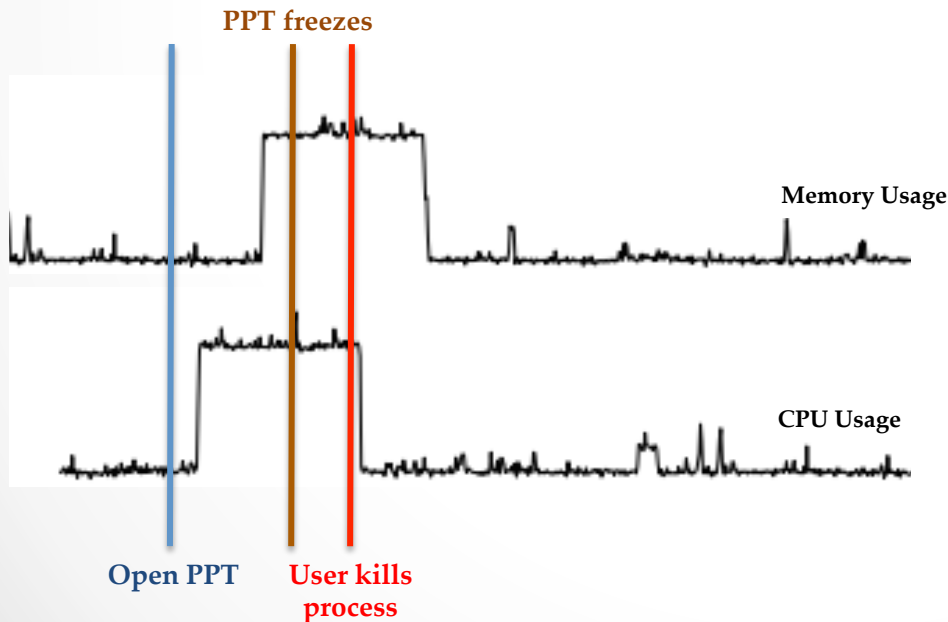
Ricardo Reimao

# Idea: Identifying Patterns in Series and Events



# Problem!

- How to correlate events with temporal series?
- How to identify anomalous behavior?
- How to predict incident causes?



Series 1: CPU Usage  
Series 2: Memory Usage  
Event Series: Windows logs

# Formalizing the Problem

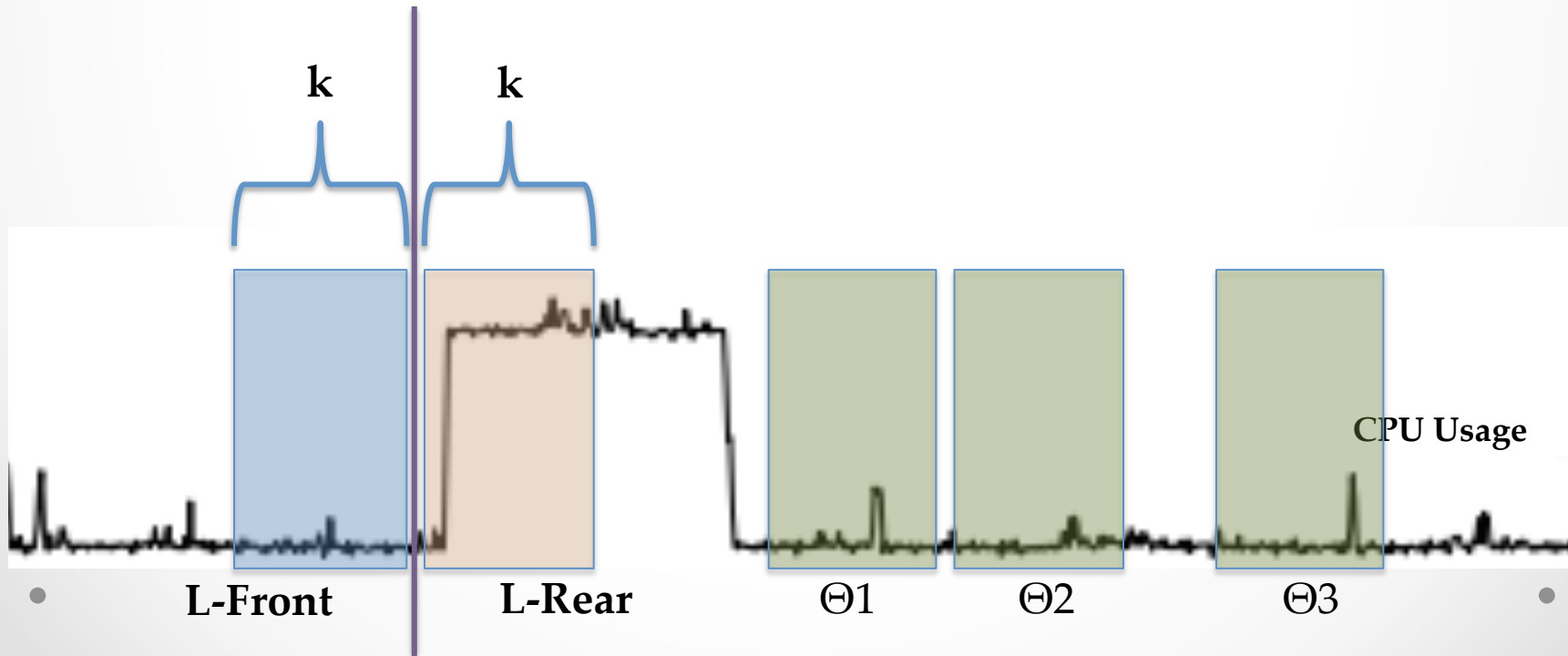
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# Three Main Questions

- Existence Dependency
  - “Is there a correlation between the event sequence and the time series?”
  - “Does opening powerpoint affect my CPU usage?”
- Temporal Order of Dependency
  - “Does X influences in Y? Or Y influences in X?”
  - “The powerpoint freezes because the memory usage is high? Or the memory usage is high because the powerpoint is frozen?”
- Monotonic Effect of Dependency
  - “Does the event impact negatively or positively on the measure?”
  - “When I open powerpoint, does the memory usage increases or decreases?”

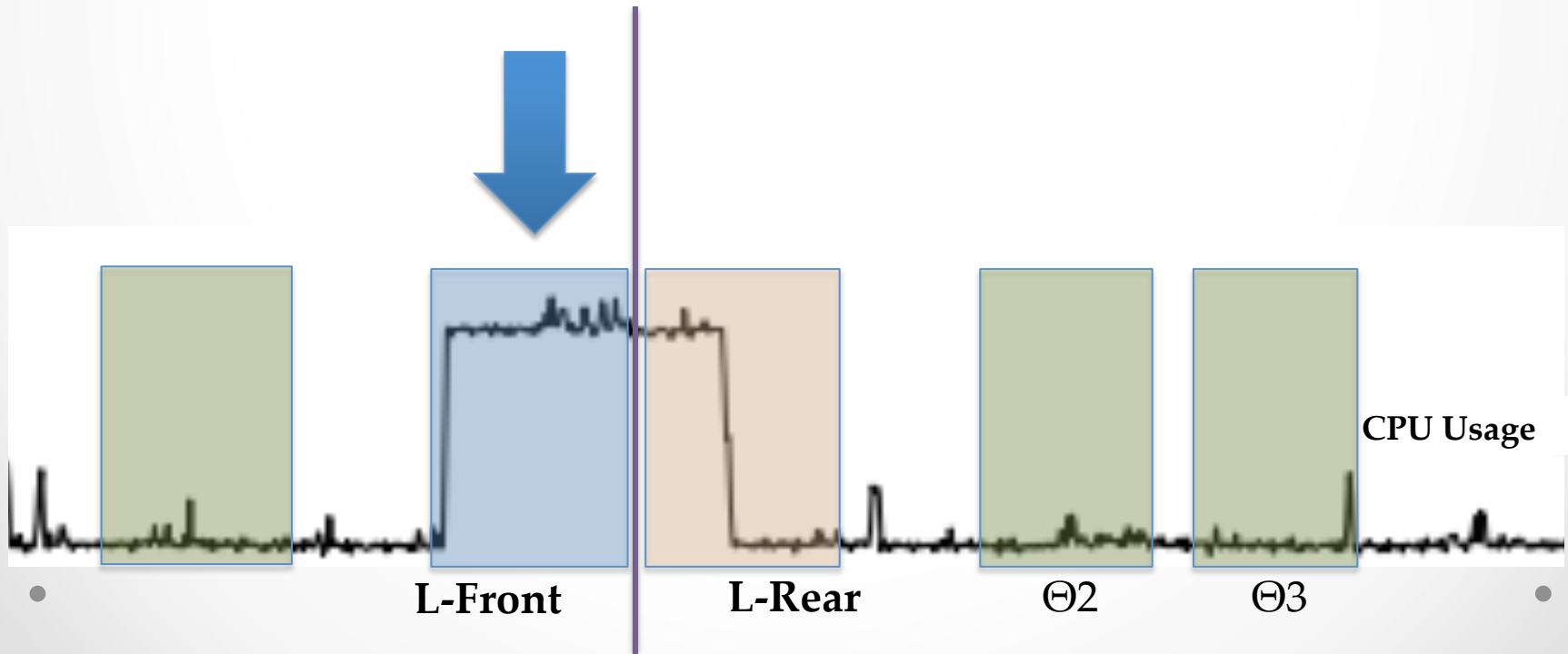
# Subset definitions

- L-Front: The sub-series BEFORE the event
- L-Rear: The sub-series AFTER the event
- $\Theta$  : A set of random sub-series
- $k$ : Size of the sub-sets



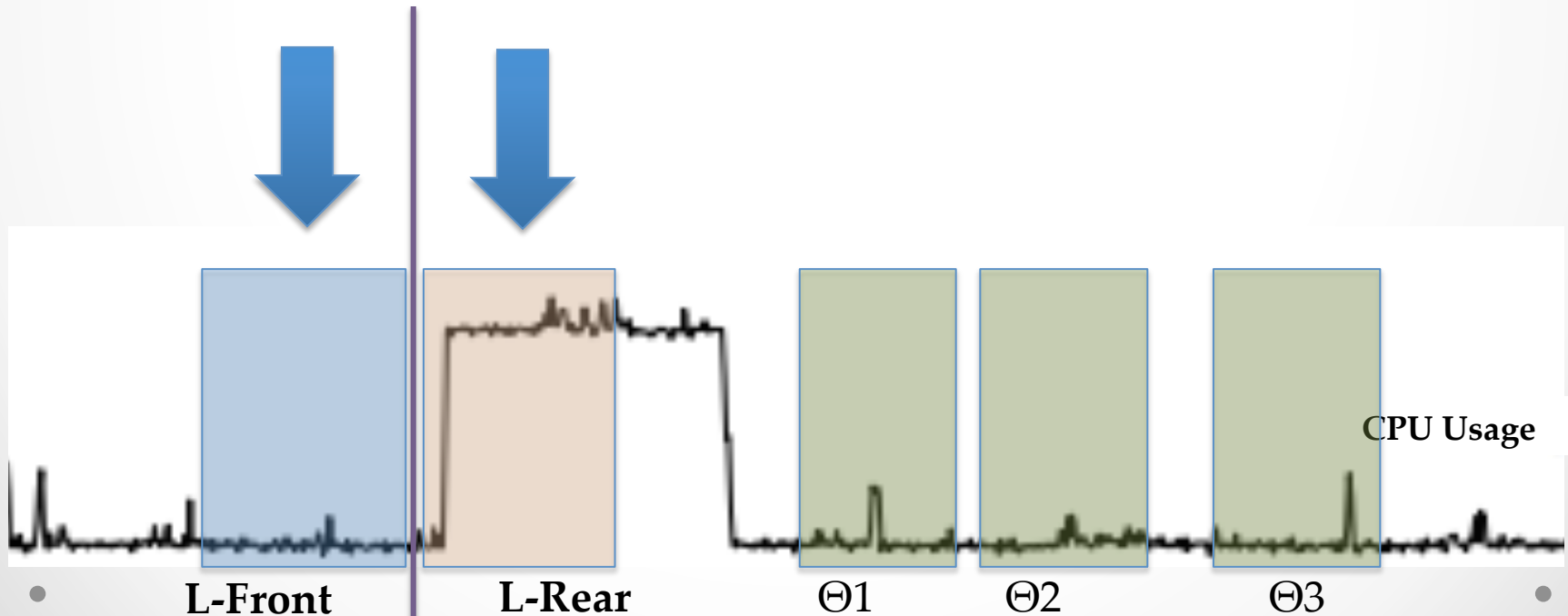
# Definition 1

- “An event sequence  $E$  and a time Series  $S$  are correlated and  $E$  often occurs **after** changes of  $S$  ( $S > E$ ) if and only if the probabilistic distribution L-Front is statistically different from the randomly sampled  $\Theta$ .



# Definition 2

- “An event sequence  $E$  and a time series  $S$  are correlated and  $E$  often occurs **before** the changes of  $S$  ( $E > S$ ), if and only if the probabilistic distribution of L-Rear is statistically different from the randomly sampled sub-series  $\Theta$  and the probabilistic distribution of L-Front is not statistically different from  $\Theta$ .”





# Definition 3

- An event sequence  $E$  and a time series  $S$  are correlated ( $E \sim S$ ) if there is a relationship such as  $E > S$  or  $S > E$

# Definition 4

- If  $E > S$  (or  $S > E$ ) and the event occurrences of  $E$  are related to significant value increases of  $S$ , we denote the correlation as  $E \rightarrow S$ .  
If  $S$  decreases, we denote the correlation as:  $E \rightarrow S$

Challenge:  
How to test if L-Rear are  
statistically similar to  $\Theta$ ?  
...

# Approach: Two Sample Problem

...

# What is Two Sample Problem?

- Multivariate two-sample hypothesis-testing problem
- Objective: Identify if two samples are from the same distribution
- In our context:
  - Check if L-Rear and  $\Theta$  are from the same distribution
  - Check if L-Front and  $\Theta$  are from the same distribution
- Two Hypothesis:
  - $H_0 : S = \Theta$  (The series and  $\Theta$  are from the same distribution, or in other words,  $S$  and  $\Theta$  are statistically equal)
  - $H_1 : S \neq \Theta$  (The series and  $\Theta$  are from different distributions, or in other words,  $S$  and  $\Theta$  are statistically different)

# How to check? Nearest Neighbor!

- Why?
- Verify the distance between an item and items in a database
- Process:
  - Generate the subset of L-Front/L-Rear
  - Generate the subset of  $\Theta$
  - Concatenate L-Front/L-Rear and  $\Theta$  (this becomes the DB)
  - Whenever a new item A (event + L-Front + L-Rear) is tested:
    - Use k-NN to check which item is more similar to A
    - If the closest item is an item of  $\Theta$ , then there's no correlation
    - Else, the item may be correlation

# Monotonicity Check

- To check the monotonic effect, a new artifact is introduced:  $t_{score}$

$$t_{score} = \frac{\mu_{\Gamma front} - \mu_{\Gamma rear}}{\sqrt{\frac{(n_1-1)\sigma_{\Gamma front}^2 + (n_2-1)\sigma_{\Gamma rear}^2}{n_1+n_2-2}} \left(\frac{1}{n_1} - \frac{1}{n_2}\right)}$$

- Idea: Measure “how big is the impact” of E in S.
- If  $t_{score}$  is higher than a threshold, then: E +> S
- If  $t_{score}$  is lower than a threshold, then: E -> S

# Algorithm

...

# Inputs/Outputs

- Input:
  - Event vector  $E = (e_1, e_2, \dots, e_n)$
  - Time Series  $S = (s_1, s_2, \dots, s_m)$
  - Subseries length  $k$
- Output:
  - Correlation flag  $C$
  - Correlation direction  $D$
  - Effect type  $t$
- Important: 'k' (subseries length) and n (number of knn neighbours to evaluate) have high impact on performance!



# General Idea

- Test L-Front and  $\Theta$
- Test L-Rear and  $\Theta$
- If correlation is found:
  - Verify  $t_{\text{score}}$  to identify direction
  - Return

---

**Algorithm 1: The Overall Algorithm**

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**Input:** Event  $E = (e_1, e_2, \dots, e_n)$ , and Time Series  
 $S = (s_1, s_2, \dots, s_m)$ , and the sub-series length  $k$ .

**Output:** The correlation flag  $C$ , the direction  $D$ , and  
the effect type  $T$

- 1 Initialize  $I^{front}$  and  $I^{rear}$ ;
  - 2 Initialize  $\Theta$ ;
  - 3 Initialize  $R = false$ ,  $D = NULL$ ,  $T = NULL$ ;
  - 4 Normalize each  $\ell_k^{front}(S, e_i)$  and  $\ell_k^{rear}(S, e_i)$ ;
  - 5 Test  $I^{front}$  and  $\Theta$  using Nearest Neighbors Method.  
The result is denoted as  $D_f$ ;
  - 6 Test  $I^{rear}$  and  $\Theta$  using Nearest Neighbors Method.  
The result is denoted as  $D_r$ ;
  - 7 if ( $D_r == true \&\& D_f == false$ ) then
    - 8  $R = true$ ;
    - 9 Calculate  $t_{score}$  using Equation (8);
    - 10 if ( $t_{score} > \alpha$ ) then
      - 11  $T = E \vec{\rightarrow} S$ ;
      - 12 else if ( $t_{score} < -\alpha$ ) then
        - 13  $T = E \overset{\pm}{\rightarrow} S$ ;
  - 14 else if ( $D_r == false \&\& D_f == true$ ) ||  
( $D_r == true \&\& D_f == true$ ) then
    - 15  $R = true$ ;
    - 16 Calculate  $t_{score}$  using Equation (8);
    - 17 if ( $t_{score} > \alpha$ ) then
      - 18  $T = S \vec{\rightarrow} E$ ;
      - 19 else if ( $t_{score} < -\alpha$ ) then
        - 20  $T = S \overset{\pm}{\rightarrow} E$ ;
  - 21 Out put  $R$ ,  $D$  and  $T$ ;
  - 22 Algorithm End.
-

# Empirical Evaluation

...

# Previous Works

- Pearson Correlation
  - One of the most used methods for measuring correlation between two time series
  - Cannot be directly used to correlate event and series data
    - Need to transform event data into a serie
- J-measure Correlation
  - One of the most used methods for measuring correlation between event data
  - Cannot be directly used to correlate event and series data
    - Need to transform series into event data

# Tests in a Controlled Environment

**Table 2: Results of the data from controlled environment**

Name	Proposed Method			Pearson Correlation			J-Measure		
	CPU	Memory	Disk	CPU	Memory	Disk	CPU	Memory	Disk
CPU Intensive Program	→	NC	NC	↔	NC <sup>1</sup>	NC	NC	~	~
Memory Intensive Program	→	→	NC	NC	↔	NC	NC	~	~
Disk Intensive Program	NC	NC	→	NC	NC	↔	NC	~	~
Query Alert	←	←	NC	↔	NC	NC	NC	~	~

- Person did not capture some correlations
- Person does not give you the direction of the correlation
- J-Measure did not identify correlation in one whole series

# Tests in Real-World Environments

Evaluation Metric:

$$F_1 = \frac{2 * TruePositive}{2 * TruePositive + FalseNegative + FalsePositive}$$

**Table 3: Result in real data set**

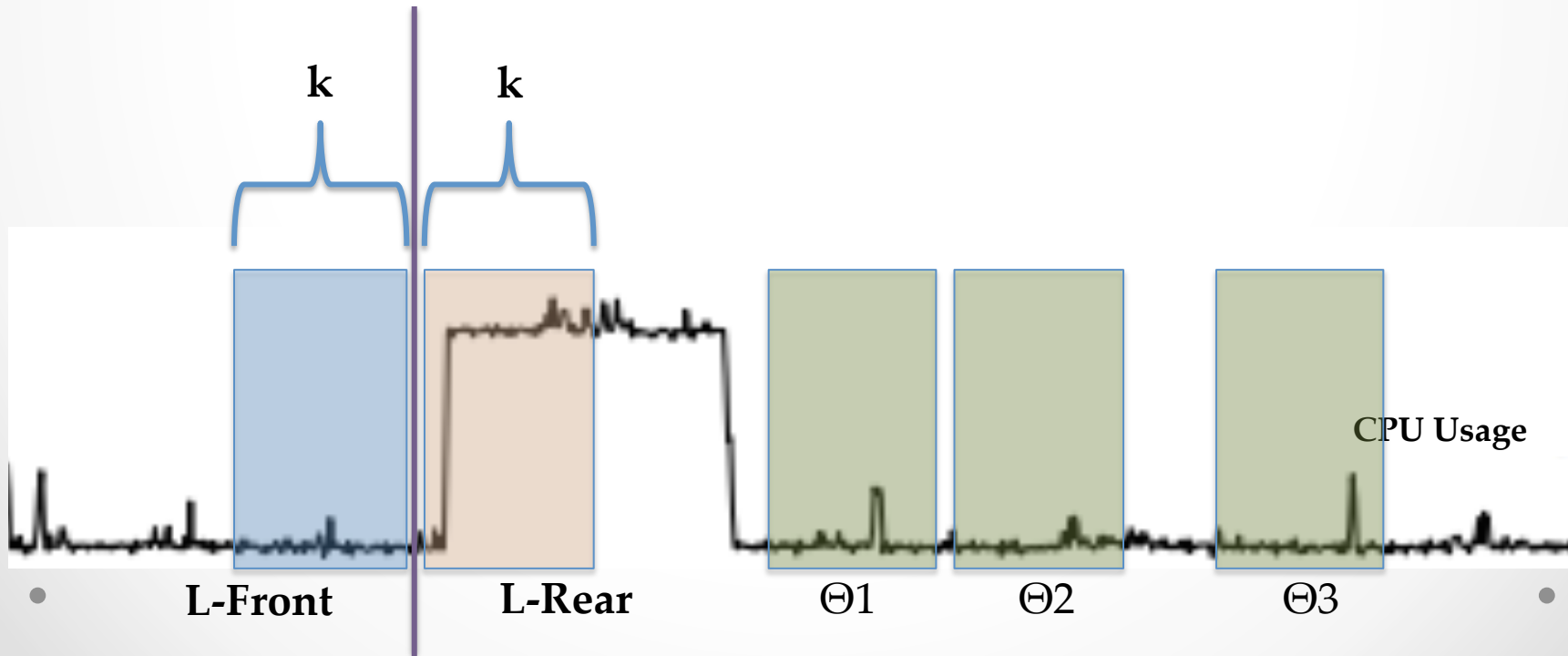
Data Set	Methods	Existence	Temporal Order	Effect Type
		$F_1$ Score	$F_1$ Score	$F_1$ Score
System Monitoring Data	Correlation Mining (L1)	0.7916	0.8020	0.8016
	Correlation Mining (L2)	<b>0.8205</b>	0.7612	<b>0.8780</b>
	Correlation Mining (DTW)	0.7962	<b>0.8021</b>	0.8210
	Pearson Correlation	0.6974	N/A <sup>2</sup>	0.6732
	J-Measure	0.6148	N/A	N/A
Custom Support Data	Correlation Mining (L1)	0.7915	0.7659	0.7204
	Correlation Mining (L2)	0.8423	0.7870	0.8334
	Correlation Mining (DTW)	<b>0.8631</b>	<b>0.8205</b>	<b>0.8532</b>
	Pearson Correlation	0.6030	N/A	0.6501
	J-Measure	0.7398	N/A	N/A

# Summary

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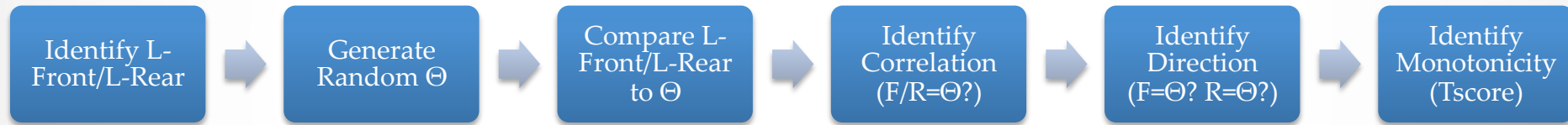
# Concept Summary

- L-Front: The sub-series BEFORE the event
- L-Rear: The sub-series AFTER the event
- $\Theta$  : A set of random sub-series
- $k$ : Size of the sub-sets





# Process



# Pros | Cons

Correlate time series and event data

Utilizes a slow-search method: Nearest Neighbors

Identify not only correlation, but also direction and monotonicity

Does not consider the event combination problem

Can be applied against multiple time series

More effective than previous works (Pearson and J-Measure)

# Questions?

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Ricardo Reimao