

Recursion

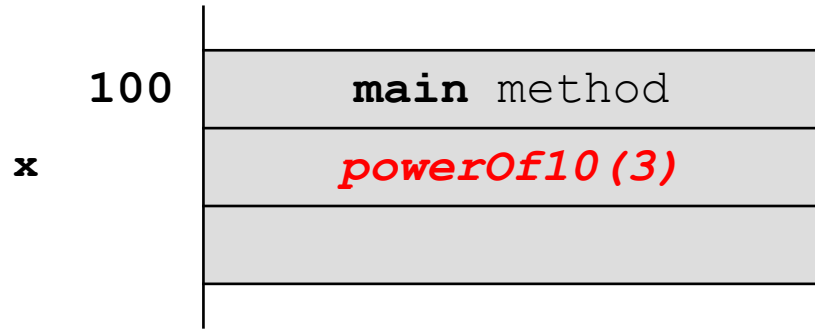
notes Chapter 8

What Happens During Recursion?

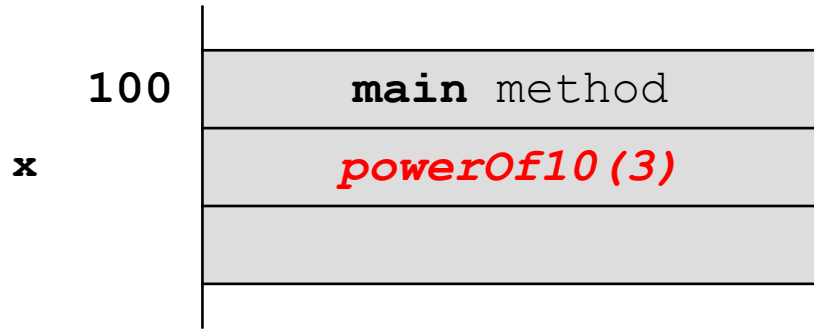
- ▶ a simplified model of what happens during a recursive method invocation is the following:
 - ▶ whenever a method is invoked that method runs in a *new* block of memory
 - ▶ when a method recursively invokes itself, a new block of memory is allocated for the newly invoked method to run in
- ▶ consider a slightly modified version of the **powerOf10** method

```
public static double powerOf10(int n) {  
    double result;  
    if (n < 0) {  
        result = 1.0 / powerOf10(-n);  
    }  
    else if (n == 0) {  
        result = 1.0;  
    }  
    else {  
        result = 10 * powerOf10(n - 1);  
    }  
    return result;  
}
```

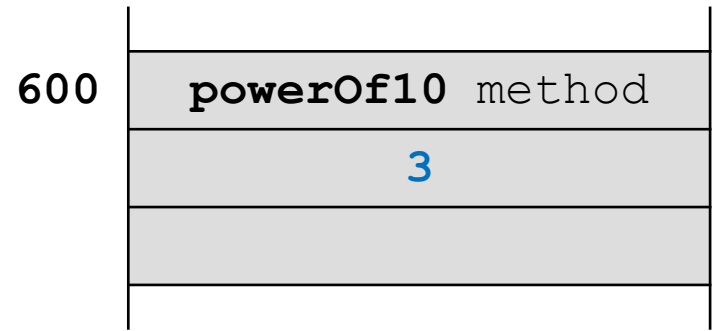
```
double x = Recursion.powerOf10(3);
```



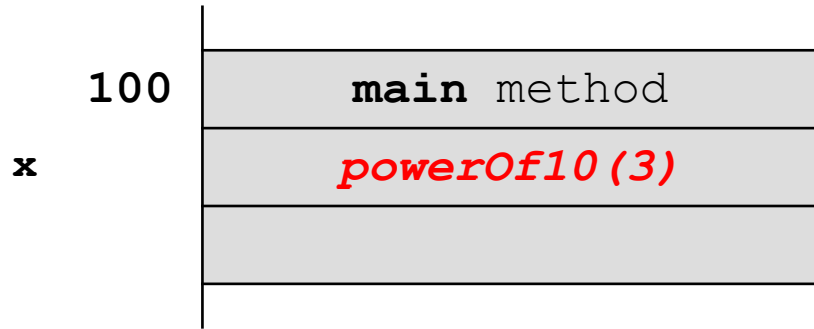
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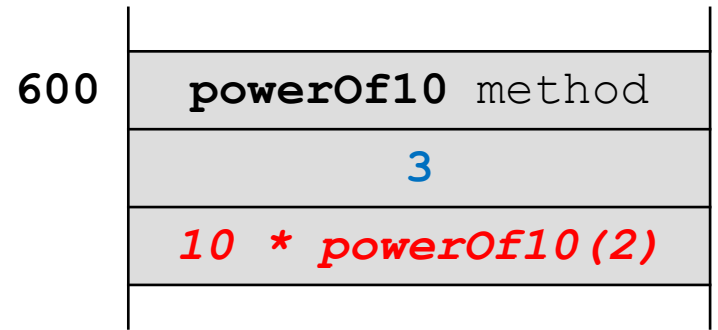
n
result



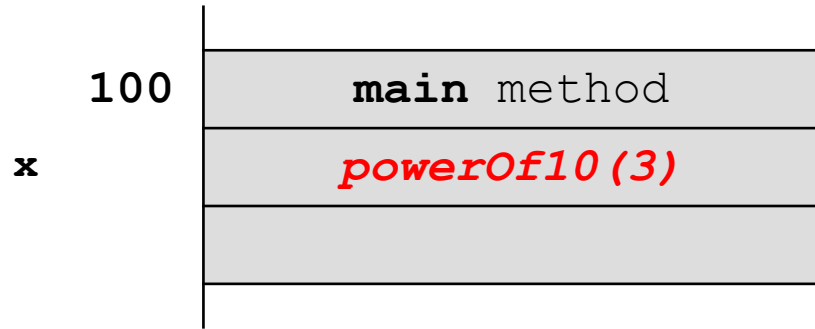
```
double x = Recursion.powerOf10(3);
```



n
result



```
double x = Recursion.powerOf10(3);
```



result

n

600

powerOf10 method

3

*10 * powerOf10(2)*

750

powerOf10 method

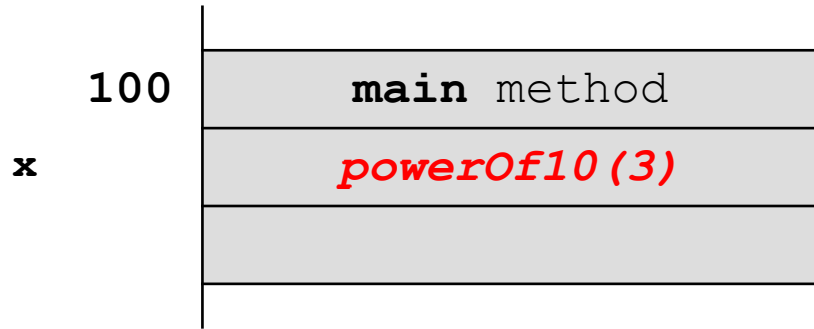
2

result

n



```
double x = Recursion.powerOf10(3);
```



result

n

600

powerOf10 method

3

$10 * \text{powerOf10}(2)$

750

powerOf10 method

2

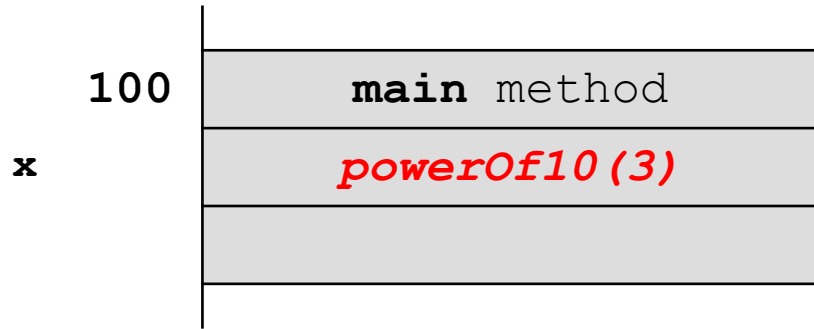
$10 * \text{powerOf10}(1)$

result

n




```
double x = Recursion.powerOf10(3);
```



result

n

600

powerOf10 method

3

$10 * \text{powerOf10}(2)$

result

n

750

powerOf10 method

2

$10 * \text{powerOf10}(1)$

result

n

800

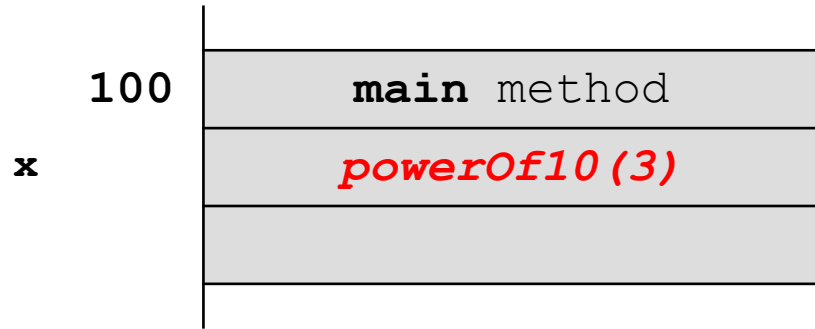
powerOf10 method

1

$10 * \text{powerOf10}(0)$



```
double x = Recursion.powerOf10(3);
```



result

600

powerOf10 method

n

3

$10 * \text{powerOf10}(2)$

result

750

powerOf10 method

n

2

$10 * \text{powerOf10}(1)$

result

800

powerOf10 method

n

1

$10 * \text{powerOf10}(0)$

result

950

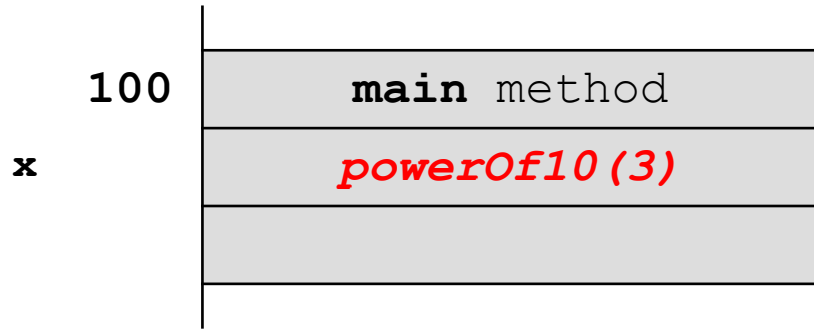
powerOf10 method

n

0



```
double x = Recursion.powerOf10(3);
```



result

600

powerOf10 method

n

3

$10 * \text{powerOf10}(2)$

result

750

powerOf10 method

n

2

$10 * \text{powerOf10}(1)$

result

800

powerOf10 method

n

1

$10 * \text{powerOf10}(0)$

result

950

powerOf10 method

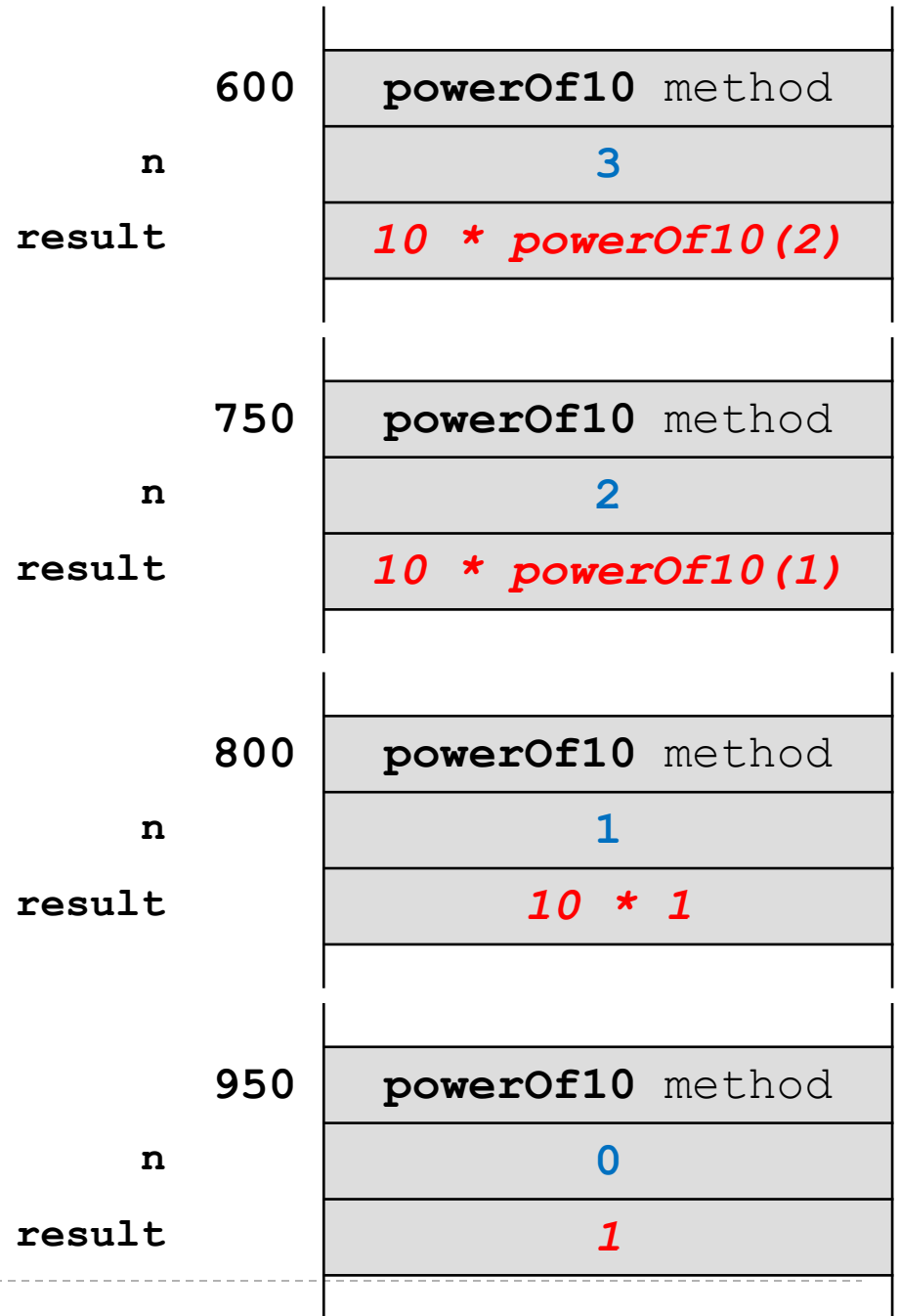
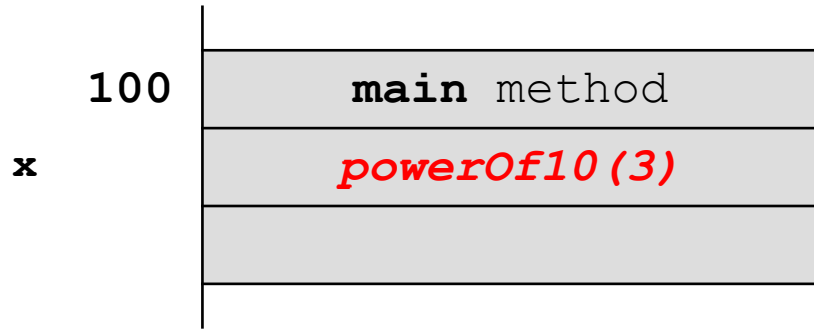
n

0

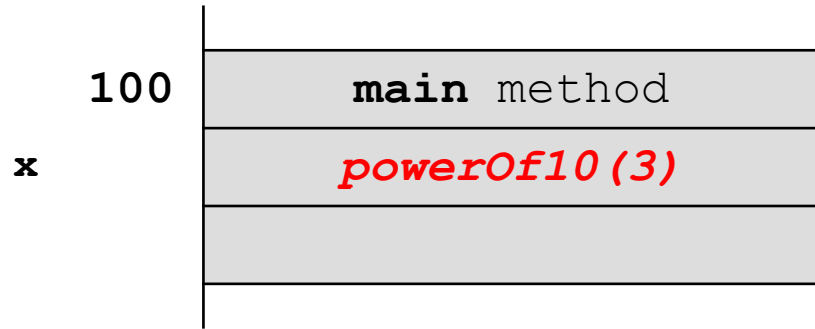
1



```
double x = Recursion.powerOf10(3);
```



```
double x = Recursion.powerOf10(3);
```



result

n

600

`powerOf10 method`

3

`10 * powerOf10(2)`

result

n

750

`powerOf10 method`

2

`10 * powerOf10(1)`

result

n

800

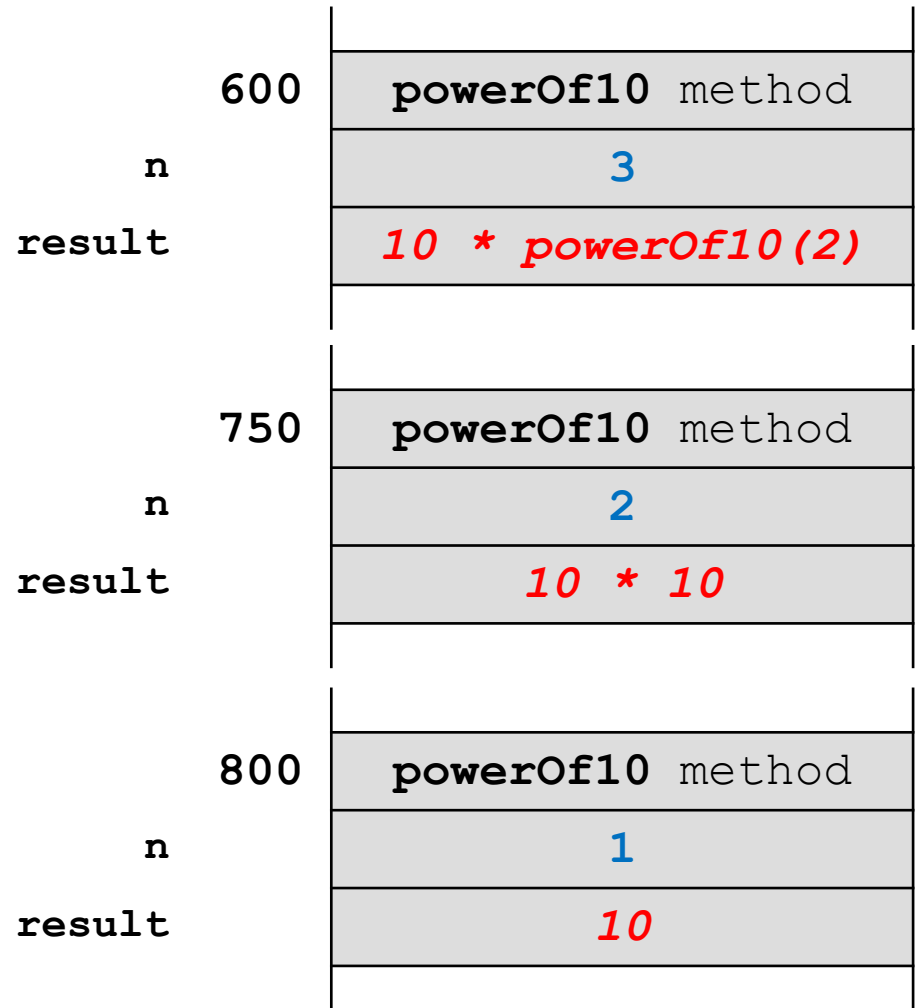
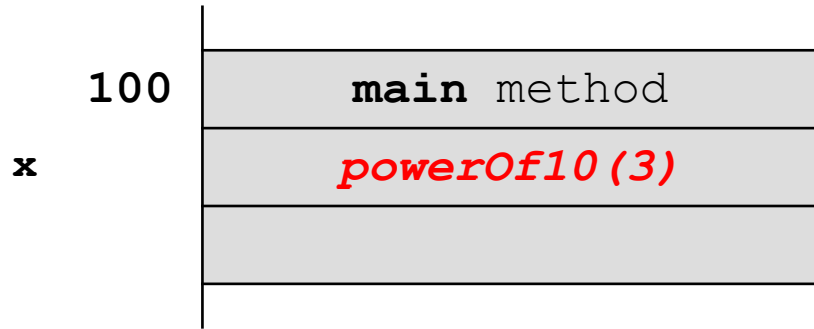
`powerOf10 method`

1

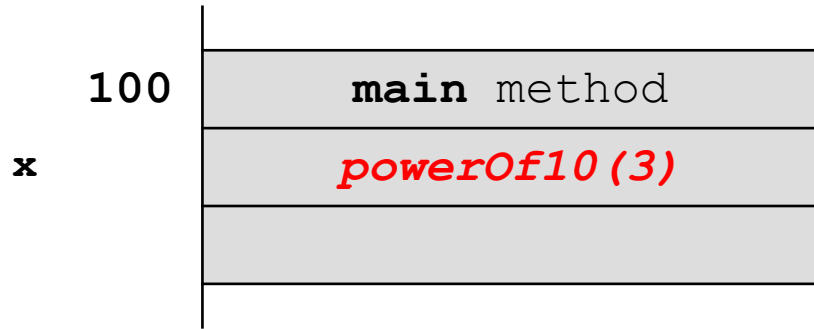
10



```
double x = Recursion.powerOf10(3);
```



```
double x = Recursion.powerOf10(3);
```



result

n

600

powerOf10 method

3

*10 * powerOf10(2)*

750

powerOf10 method

2

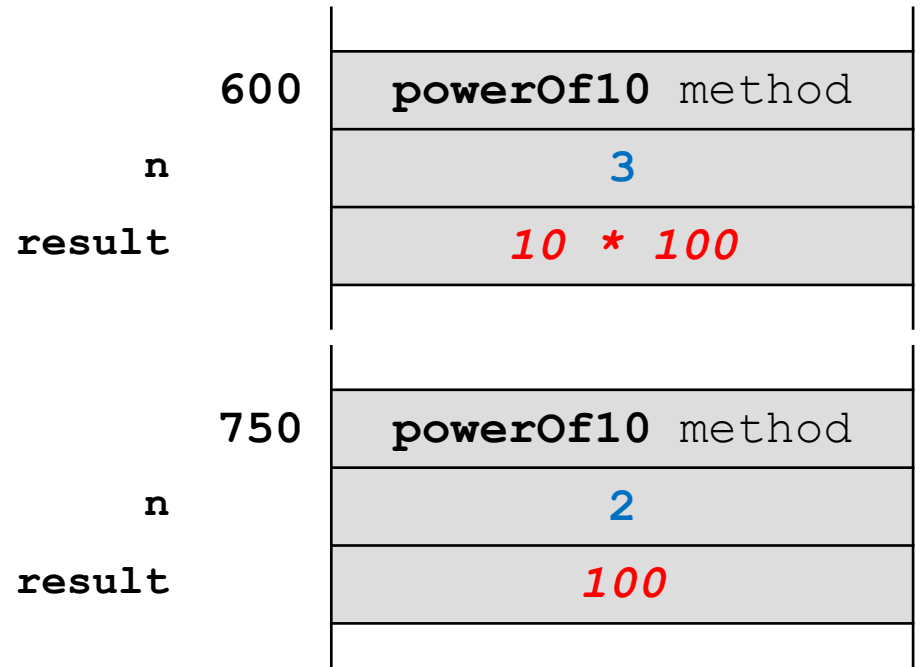
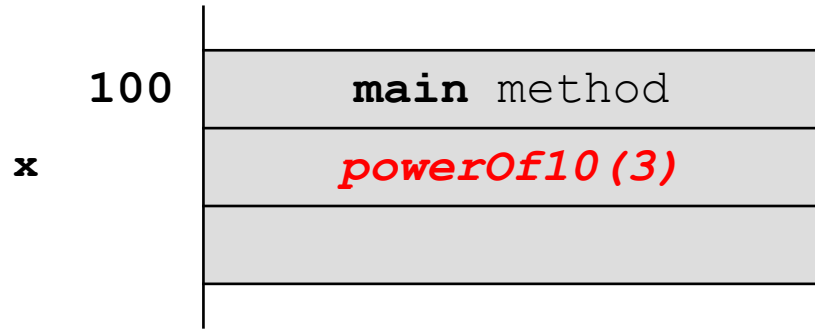
100

result

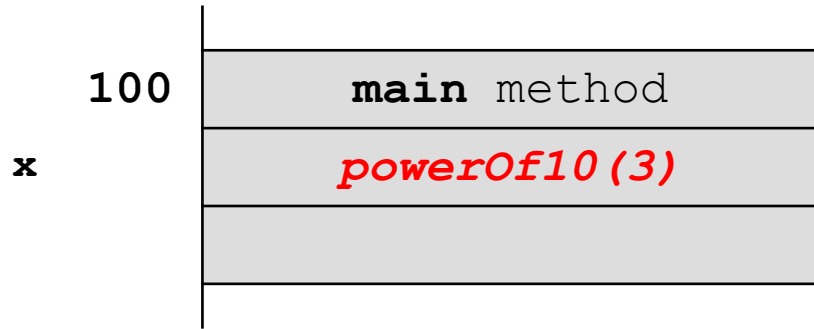
n



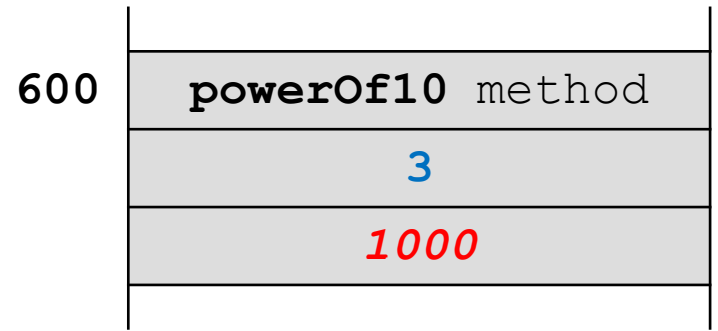
```
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```



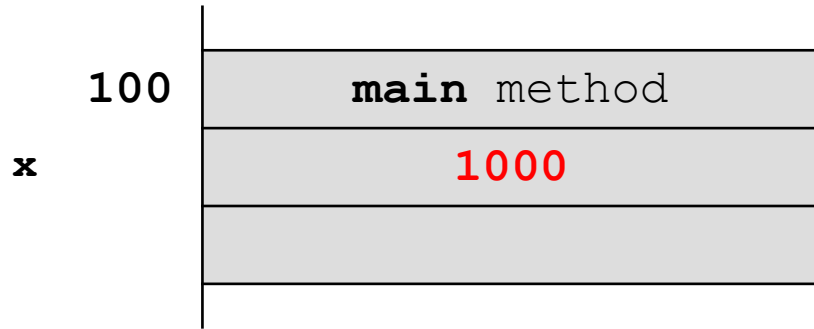

```
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```



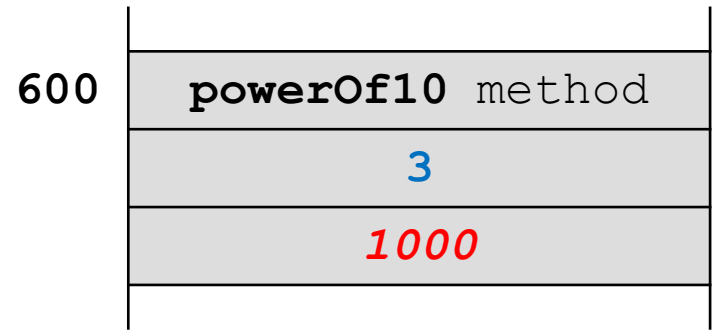
n
result



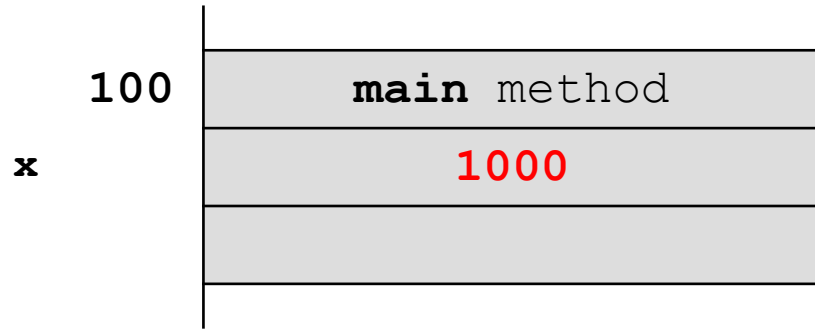
```
double x = Recursion.powerOf10(3);
```



n
result



```
double x = Recursion.powerOf10(3);
```



Recursion and Collections

- ▶ consider the problem of searching for an element in a list
- ▶ searching a list for a particular element can be performed by recursively examining the first element of the list
 - ▶ if the first element is the element we are searching for then we can return true
 - ▶ otherwise, we recursively search the sub-list starting at the next element
- ▶ example:
search for "X" in the list ["Z", "Q", "B", "X", "J"]

Recursively Search a List

`contains("X", ["Z", "Q", "B", "X", "J"])`

→ `"X".equals("Z") == false`

→ `contains("X", ["Q", "B", "X", "J"])` recursive call

→ `"X".equals("Q") == false`

→ `contains("X", ["B", "X", "J"])` recursive call

→ `"X".equals("B") == false`

→ `contains("X", ["X", "J"])` recursive call

→ `"X".equals("X") == true` done!

Recursively Search a List

- ▶ base case(s)?

```
public class Day25 {
```

```
public static <T> boolean contains(T element, List<T> t) {  
    boolean result;
```

```
    if (t.size() == 0) { // base case  
        result = false;  
    }
```

```
    else if (t.get(0).equals(element)) { // base case  
        result = true;  
    }
```

```
}
```

```
}
```

Recursively Search a List

- ▶ recursive call?


```
public class Day25 {
```

```
public static <T> boolean contains(T element, List<T> t) {
```

```
    boolean result;
```

```
    if (t.size() == 0) { // base case
```

```
        result = false;
```

```
    }
```

```
    else if (t.get(0).equals(element)) { // base case
```

```
        result = true;
```

```
    }
```

```
    else { // recursive call
```

```
        result = Day25.contains(element, t.subList(1, t.size()));
```

```
    }
```

```
    return result;
```

```
}
```

```
}
```

Recursion and Collections

- ▶ consider the problem of moving the smallest element in a list of integers to the front of the list

Recursively Move Smallest to Front

8	7	6	4	3	5	0	2	9	1
---	---	---	---	---	---	---	---	---	---

original list

8	7	6	4	3	5	0	2	9	1
---	---	---	---	---	---	---	---	---	---

recursion

move the smallest element of this sublist to the front of the sublist

8	0
---	---	-----	-----	-----	-----	-----	-----	-----	-----

compare



compare these two elements and move the smallest one to the front (swapping positions)

0	8
---	---	-----	-----	-----	-----	-----	-----	-----	-----

updated list



Recursively Move Smallest to Front

- ▶ base case?

Recursively Move Smallest to Front

```
public class Day25 {
```

```
    public static void minToFront(List<Integer> t) {
```

```
        if (t.size() < 2) {
```

```
            return;
```

```
        }
```

```
    }
```

```
}
```

Recursively Move Smallest to Front

- ▶ recursive call?

Recursively Move Smallest to Front

```
public class Day25 {
```

```
    public static void minToFront(List<Integer> t) {  
        if (t.size() < 2) {  
            return;  
        }  
    }
```

```
        Day25.minToFront(t.subList(1, t.size()));
```

<http://docs.oracle.com/javase/7/docs/api/java/util/List.html#subList%28int,%20int%29>

```
    }
```

```
}
```



Recursively Move Smallest to Front

- ▶ compare and update?

Recursively Move Smallest to Front

```
public class Day25 {  
  
    public static void minToFront(List<Integer> t) {  
        if (t.size() < 2) {  
            return;  
        }  
        Day25.minToFront(t.subList(1, t.size()));  
  
        int first = t.get(0);  
        int second = t.get(1);  
        if (second < first) {  
            t.set(0, second);  
            t.set(1, first);  
        }  
    }  
}
```