...

- 1		The <u>situation calculus</u> is a dialect of FOL for representing dynamically changing worlds in which all changes are the result of named actions.
14.		There are two distinguished sorts of terms:
Actions		<ul> <li><u>actions</u>, such as <ul> <li>put(x,y) put object x on top of object y</li> <li>walk(loc) walk to location loc</li> <li>pickup(r,x) robot r picks up object x</li> </ul> </li> <li><u>situations</u>, denoting possible world histories. A distinguished constant S<sub>0</sub> and function symbol do are used <ul> <li>S<sub>0</sub> the initial situation, before any actions have been performed</li> <li>do(a,s) the situation that results from doing action a in situation s</li> </ul> </li> </ul>
		for example: $do(put(A,B), do(put(B,C),S_0))$ the situation that results from putting A on B after putting B on C in the initial situation
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.. ..

. . .

### Fluents

Predicates or functions whose values may vary from situation to situation are called <u>fluents</u>.

These are written using predicate or function symbols whose last argument is a situation

- for example: Holding(r, x, s): robot r is holding object x in situation s
- can have:  $\neg$ Holding(r, x, s)  $\land$  Holding(r, x, do(pickup(r, x),s))

the robot is not holding the object x in situation s, but is holding it in the situation that results from picking it up

**Note**: there is no distinguished "current" situation. A sentence can talk about many different situations, past, present, or future.

A distinguished predicate symbol Poss(a,s) is used to state that a may be performed in situation s

for example:	$Poss(pickup(r,x), S_0)$
--------------	--------------------------

This is the entire language.

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it is possible for the robot *r* to pickup object *x* in the initial situation

### **Preconditions and effects**

It is necessary to include in a KB not only facts about the initial situation, but also about world dynamics: what the actions do.

Actions typically have <u>preconditions</u>: what needs to be true for the action to be performed

 Poss(pickup(r,x), s) = ∀z. ¬Holding(r,z,s) ∧ ¬Heavy(x) ∧ NextTo(r,x,s) a robot can pickup an object iff it is not holding anything, the object is not too heavy, and the robot is next to the object

Note: free variables assumed to be universally quantified

•  $Poss(repair(r,x), s) = HasGlue(r,s) \land Broken(x,s)$ 

it is possible to repair an object iff the object is broken and the robot has glue

Actions typically have <u>effects</u>: the fluents that change as the result of performing the action

- Fragile(x)  $\supset$  Broken(x, do(drop(r,x),s))
  - dropping a fragile object causes it to break
- $\neg$  Broken(x, do(repair(r,x),s))

repairing an object causes it to be unbroken

### The frame problem

To really know how the world works, it is also necessary to know what fluents are *unaffected* by performing an action.

- Colour(x, c, s) ⊃ Colour(x, c, do(drop(r,x),s)) dropping an object does not change its colour
- ¬Broken(x,s) ∧ [x≠y ∨ ¬Fragile(x)] ⊃ ¬Broken(x, do(drop(r,y),s) not breaking things

These are sometimes called frame axioms.

**Problem**: need to know a vast number of such axioms. (Few actions affect the value of a given fluent; most leave it invariant.)

an object's colour is unaffected by picking things up, opening a door, using the phone, turning on a light, electing a new Prime Minister of Canada, *etc.* 

The frame problem:

- in building KB, need to think of these ~ 2 × A × F facts about what does not change
- the system needs to reason efficiently with them

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241

### What counts as a solution?

 Suppose the person responsible for building a KB has written down all the effect axioms

for each fluent *F* and action *A* that can cause the truth value of *F* to change, an axiom of the form  $[R(s) \supset \pm F(do(A,s))]$ , where R(s) is some condition on *s* 

- We want a systematic procedure for generating all the frame axioms from these effect axioms
- If possible, we also want a *parsimonious* representation for them (since in their simplest form, there are too many)

Why do we want such a solution?

- frame axioms are necessary to reason about actions and are not entailed by the other axioms
- convenience for the KB builder
   for theorizing about actions
   modularity: only add effect axioms
   accuracy: no inadvertent omissions

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242

### The projection task

What can we do with the situation calculus?

We will see later that it can be used for planning.

A simpler job we can handle directly is called the projection task.

Given a sequence of actions, determine what would be true in the situation that results from performing that sequence.

This can be formalized as follows:

Suppose that R(s) is a formula with a free situation variable s.

To find out if R(s) would be true after performing  $\langle a_1,...,a_n \rangle$  in the initial situation, we determine whether or not

 $KB \mid = R(do(a_n, do(a_{n-1}, ..., do(a_1, S_0)...)))$ 

For example, using the effect and frame axioms from before, it follows that  $\neg$ Broken(B,*s*) would hold after doing the sequence

 $\langle pickup(A), pickup(B), drop(B), repair(B), drop(A) \rangle$ 

The legality task

The projection task above asks if a condition would hold after performing a sequence of actions, but not whether that sequence can in fact be properly executed.

We call a situation <u>legal</u> if it is the initial situation or the result of performing an action whose preconditions are satisfied starting in a legal situation.

The <u>legality task</u> is the task of determining whether a sequence of actions leads to a legal situation.

This can be formalized as follows:

To find out if the sequence  $\langle a_1,...,a_n \rangle$  can be legally performed in the initial situation, we determine whether or not

 $KB \mid = Poss(a_i, do(a_{i-1}, ..., do(a_1, S_0)...))$ 

for every *i* such that  $1 \le i \le n$ .

### Limitations of the situation calculus

This version of the situation calculus has a number of limitations:

- no time: cannot talk about how long actions take, or when they occur
- only known actions: no hidden exogenous actions, no unnamed events
- · no concurrency: cannot talk about doing two actions at once
- only discrete situations: no continuous actions, like pushing an object from A to B.
- only hypotheticals: cannot say that an action has occurred or will occur
- only primitive actions: no actions made up of other parts, like conditionals or iterations

We will deal with the last of these below.

First we consider a simple solution to the frame problem ...

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245

### Normal form for effect axioms

Suppose there are two positive effe	ct axioms for the fluent Broken:
$Fragile(x) \supset Broken(x, do(drop(r, x), x))$	s))
NextTo( $b,x,s$ ) $\supset$ Broken( $x,do(explose)$	de(b),s))
These can be rewritten as	
$\exists r \{a = \operatorname{drop}(r, x) \land \operatorname{Fragile}(x)\} \lor \exists b \\ \supset \operatorname{Broken}(x, do(a, s))$	$\{a = \exp[ode(b) \land \operatorname{NextTo}(b, x, s)\}$
Similarly, consider the negative effe	ect axiom:
$\neg$ Broken(x,do(repair(r,x),s))	
which can be rewritten as	
$\exists r \{a = \operatorname{repair}(r, x)\} \supset \neg \operatorname{Broken}(x, deta)$	p(a,s))
In general, for any fluent $F$ , we can as two formulas of the form	rewrite all the effect axioms as
$P_{F}(\boldsymbol{x}, a, s) \supset F(\boldsymbol{x}, do(a, s)) $ (1)	where $P_F(x, a, s)$ and $N_F(x, a, s)$
$N_{F}(\boldsymbol{x}, a, s) \supset \neg F(\boldsymbol{x}, do(a, s)) $ (2)	are among the $x_i$ , $a$ , and $s$ .

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246

### **Explanation closure**

Now make a completeness assumption regarding these effect axioms:

assume that (1) and (2) characterize all the conditions under which an action a changes the value of fluent F.

This can be formalized by explanation closure axioms:

 $\neg F(\mathbf{x}, s) \land F(\mathbf{x}, do(a,s)) \supset P_{F}(\mathbf{x}, a, s)$ (3) if *F* was false and was made true by doing action *a* then condition  $P_{F}$  must have been true

 $F(\mathbf{x}, s) \wedge \neg F(\mathbf{x}, do(a, s)) \supset \mathcal{N}_{\mathsf{F}}(\mathbf{x}, a, s) \tag{4}$ 

if F was true and was made false by doing action a then condition  $\rm N_F$  must have been true

These explanation closure axioms are in fact disguised versions of frame axioms!

$$\neg F(\mathbf{x}, s) \land \neg \mathbf{P}_{\mathbf{F}}(\mathbf{x}, a, s) \supset \neg F(\mathbf{x}, do(a, s))$$
  
 
$$F(\mathbf{x}, s) \land \neg \mathbf{N}_{\mathbf{F}}(\mathbf{x}, a, s) \supset F(\mathbf{x}, do(a, s))$$

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### Successor state axioms

Further assume that our KB entails the following

• integrity of the effect axioms:  $\neg \exists x, a, s$ .  $P_F(x, a, s) \land N_F(x, a, s)$ 

· unique names for actions:

 $\begin{array}{l} A(x_1,...,x_n) = A(y_1,...,y_n) \supset (x_1 = y_1) \land ... \land (x_n = y_n) \\ A(x_1,...,x_n) \neq B(y_1,...,y_m) \quad \text{where } A \text{ and } B \text{ are distinct} \end{array}$ 

Then it can be shown that KB entails that (1), (2), (3), and (4) together are logically equivalent to

$$F(\mathbf{x}, do(a,s)) = P_{F}(\mathbf{x}, a, s) \lor (F(\mathbf{x}, s) \land \neg N_{F}(\mathbf{x}, a, s))$$

This is called the <u>successor state axiom</u> for *F*.

For example, the successor state axiom for the Broken fluent is:

Broken(x, $do(a,s)$ ) = $\exists r \{a = \operatorname{drop}(r,x) \land \operatorname{Fragile}(x)\}$ $\lor \exists b \{a = \exp[\operatorname{ode}(b) \land \operatorname{NextTo}(b,x,s)\}$ $\lor \operatorname{Broken}(x, s) \land \neg \exists r \{a = \operatorname{repair}(r,x)\}$ Note universal quantification: for any action a	An object <i>x</i> is broken after doing action <i>a</i> iff <i>a</i> is a dropping action and <i>x</i> is fragile, or <i>a</i> is a bomb exploding where <i>x</i> is next to the bomb, or <i>x</i> was already broken and <i>a</i> is not the action of repairing it
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### A simple solution to the frame problem

This simple solution to the frame problem (due to Ray Reiter) yields the following axioms:	
one successor state axiom per fluent	
<ul> <li>one precondition axiom per action</li> </ul>	
<ul> <li>unique name axioms for actions</li> </ul>	
Moreover, we do not get fewer axioms at the expense of prohibitively long ones	
the length of a successor state axioms is roughly proportional to the number of actions which affect the truth value of the fluent	
The conciseness and perspicuity of the solution relies on	
quantification over actions	
the assumption that relatively few actions affect each fluent	
<ul> <li>the completeness assumption (for effects)</li> </ul>	
Moreover, the solution depends on the fact that actions always	

have deterministic effects.

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249

### Limitation: primitive actions

As yet we have no way of handling in the situation calculus complex actions made up of other actions such as

- conditionals: If the car is in the driveway then drive else walk
- iterations: while there is a block on the table, remove one
- nondeterministic choice: pickup up some block and put it on the floor
   and others

Would like to *define* such actions in terms of the primitive actions, and inherit their solution to the frame problem

Need a compositional treatment of the frame problem for complex actions

Results in a novel programming language for discrete event simulation and high-level robot control

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250

### The Do formula

For each complex action A, it is possible to define a formula of the situation calculus, Do(A, s, s'), that says that action A when started in situation s may legally terminate in situation s'.

Primitive actions:  $Do(A, s, s') = Poss(A, s) \land s' = do(A, s)$ 

Sequence:  $Do([A;B], s, s') = \exists s''. Do(A, s, s'') \land Do(B, s'', s')$ 

Conditionals: 
$$Do([if \phi then A else B], s, s') = \phi(s) \land Do(A, s, s') \lor \neg \phi(s) \land Do(B, s, s')$$

Nondeterministic branch:  $Do([A | B], s, s') = Do(A, s, s') \vee Do(B, s, s')$ 

Nondeterministic choice:  $Do([\pi x. A], s, s') = \exists x. Do(A, s, s')$ 

etc.

**Note**: programming language constructs with a purely logical situation calculus interpretation

### GOLOG

<u>GOLOG</u> (Algol in <u>log</u>ic) is a programming language that generalizes conventional imperative programming languages

- the usual imperative constructs + concurrency, nondeterminism, more...
- bottoms out *not* on operations on internal states (assignment statements, pointer updates) but on *primitive actions* in the world (*e.g.* pickup a block)
- what the primitive actions do is user-specified by precondition and successor state axioms

### What does it mean to "execute" a GOLOG program?

- find a sequence of primitive actions such that performing them starting in some initial situation *s* would lead to a situation *s'* where the formula *Do(A, s, s')* holds
- give the sequence of actions to a robot for actual execution in the world

### **Note**: to find such a sequence, it will be necessary to reason about the primitive actions

A; if Holding(x) then B else C

to decide between B and C we need to determine if the fluent *Holding* would be true after doing A

### **GOLOG** example

Primitive actions: pickup(x	(x), putonfloor(x), putontable(x)
Fluents: Holding(x,s), OnT	Table(x,s), $OnFloor(x,s)$
Action preconditions: Poss	$(\operatorname{pickup}(x), s) = \forall z. \neg \operatorname{Holding}(z, s)$
Poss	(putonfloor(x), s) = Holding(x, s)
Poss	(putontable(x), s) = Holding(x, s)
Successor state axioms:	
Holding(x, do(a,s)) = a = pi   Holding   OnTable(x, do(a,s)) = a = p   OnFloor(x, do(a,s)) = a = p	$ckup(x) \lor$ $(x,s) \land a \neq putontable(x) \land a \neq putonfloor(x)$ $utontable(x) \lor OnTable(x,s) \land a \neq pickup(x)$ $utonfloor(x) \lor OnFloor(x,s) \land a \neq pickup(x)$
Initial situation: $\forall x. \neg Ho$	$lding(x, S_0)$
OnTable	$c(x, S_0) = x = A \lor x = B$

### Complex actions:

*proc* ClearTable : *while*  $\exists b$ .OnTable(*b*) *do*  $\pi b$  [OnTable(*b*)? ; RemoveBlock(*b*)] *proc* RemoveBlock(*x*) : pickup(*x*) ; putonfloor(*x*)

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### **Running GOLOG**

To find program	a sequence of actions constituting a legal execution of a GO n, we can use Resolution with answer extraction.	LOG
For the	above example, we have	
K	$\exists  = \exists s. Do(ClearTable, S_0, s)$	
The res	sult of this evaluation yields	
<i>s</i> :	= do(putonfloor(B), do(pickup(B), do(putonfloor(A), do(pickup(A)	$(S_0))))$
and so	a correct sequence is	
ζt	ickup(A), putonfloor(A), pickup(B), putonfloor(B)	
When was Horn	what is known about the actions and initial state can be expre	ssed
The	GOLOG interpreter in Prolog has clauses like	
	<pre>do(A,S1,do(A,S1)) :- prim_action(A), poss(A,S1).</pre>	
	<pre>do(seq(A,B),S1,S2) :- do(A,S1,S3), do(B,S3,S2).</pre>	
This pr	ovides a convenient way of controlling a robot at a high level.	
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### Planning

So far, in looking at actions, we have considered how an agent could figure out what to do given a high-level program or complex action to execute.

Now, we consider a related but more general reasoning problem: figure out what to do to make an arbitrary condition true. This is called planning.

- · the condition to be achieved is called the goal
- the sequence of actions that will make the goal true is called the plan

Plans can be at differing levels of detail, depending on how we formalize the actions involved

• "do errands" vs. "get in car at 1:32 PM, put key in ignition, turn key clockwise, change gears,..."

In practice, planning involves anticipating what the world will be like, but also observing the world and replanning as necessary...

# 15.

## Planning

### Using the situation calculus

The situation calculus can be used to represent what is known about the current state of the world and the available actions.

The planning problem can then be formulated as follows:

Given a formula Goal(s), find a sequence of actions *a* such that

 $KB \models Goal(do(\boldsymbol{a}, S_0)) \land Legal(do(\boldsymbol{a}, S_0))$ 

where  $do(\langle a_1,...,a_n\rangle, S_0)$  is an abbreviation for

 $do(a_n, do(a_{n-1}, ..., do(a_2, do(a_1, S_0)) ...))$ 

and where  $Legal(\langle a_1,...,a_n\rangle, S_0)$  is an abbreviation for

 $Poss(a_1, S_0) \land Poss(a_2, do(a_1, S_0)) \land \dots \land Poss(a_n, do(\langle a_1, \dots, a_{n-1} \rangle, S_0))$ 

So: given a goal formula, we want a sequence of actions such that

**Deriving a plan** 

- the goal formula holds in the situation that results from executing the actions, and
- it is possible to execute each action in the appropriate situation

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257

### Planning by answer extraction

Having formulated planning in this way, we can use Resolution with answer extraction to find a sequence of actions:

 $KB \models \exists s. Goal(s) \land Legal(s)$ 

We can see how this will work using a simplified version of a previous example:

An object is on the table that we would like to have on the floor. Dropping it will put it on the floor, and we can drop it, provided we are holding it. To hold it, we need to pick it up, and we can always do so.

KB

- Effects: OnFloor(x, do(drop(x),s)) Holding(x, do(pickup(x),s)) Note: ignoring frame problem
- Preconds: Holding $(x, s) \supset Poss(drop(x), s)$ Poss(pickup(x), s)
- Initial state: OnTable(B, S<sub>0</sub>)

• The goal: OnFloor(B, s)

```
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```

258

### Negated query + answer predicate Axiom 1 $[\neg OnFloor(B,sl), \neg Legal(s1), A(sl)]$ expand Legal $[\neg Legal(do(drop(B),s2)), A(do(drop(B),s2))]$ Axiom 3 [¬Legal(s2), ¬Poss(drop(B),s2), A(do(drop(B),s2))] Axiom 2 [¬Legal(s2), ¬Holding(B,s2), A(do(drop(B),s2))] [A(do(drop(B),do(pickup(B),s3))), ¬Legal(do(pickup(B),s3))] expand Legal [¬Legal(s3), A(do(drop(B),do(pickup(B),s3))), ¬Poss(pickup(B),s3), ] Axiom 4 [¬Legal(s3), A(do(drop(B),do(pickup(B),s3)))] Legal for $S_{\alpha}$ [A(do(drop(B), do(pickup(B), S0)))] Here is the plan: in the initial situation, pickup block B, and in the resulting situation, drop B. KR & R © Brachman & Levesque 2005 259

### **Using Prolog**

Because all the required facts here can be expressed as Horn clauses, we can use Prolog directly to synthesize a plan:

```
onfloor(X,do(drop(X),S)).
holding(X,do(pickup(X),S)).
poss(drop(X),S) := holding(X,S).
poss(pickup(X),S).
ontable(b,s0).
legal(s0).
legal(do(A,S)) := poss(A,S), legal(S).
```

With the Prolog goal	<pre>?- onfloor(b,S), legal(S).</pre>
we get the solution	<pre>S = do(drop(b),do(pickup(b),s0))</pre>
But planning problems	are rarely this easy!

Full Resolution theorem-proving can be problematic for a complex set of axioms dealing with actions and situations explicitly...

### The STRIPS representation

STRIPS is an alternative representation to the pure situation calculus for planning.

from work on a robot called Shaky at SRI International in the 60's.

In STRIPS, we do not represent histories of the world, as in the situation calculus.

Instead, we deal with a single world <u>state</u> at a time, represented by a database of ground atomic wffs (e.g.,  $In(robot, room_1)$ )

This is like the database of facts used in procedural representations and the working memory of production systems

Similarly, we do not represent actions as part of the world model (cannot reason about them directly), as in the situation calculus.

Instead, actions are represented by <u>operators</u> that syntactically transform world models

An operator takes a DB and transforms it to a new DB

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261

### **STRIPS** operators

Operators have pre- and post-conditions
precondition = formulas that need to be true at start
"delete list" = formulas to be removed from DB
"add list" = formulas to be added to DB

**Example**: PushThru(o,d, $r_1$ , $r_2$ )

"the robot pushes object *o* through door *d* from room  $r_1$  to room  $r_2$ "

- precondition: InRoom(robot,  $r_1$ ), InRoom( $o, r_1$ ), Connects( $d, r_1, r_2$ )
- delete list: InRoom(robot, $r_1$ ), InRoom( $o, r_1$ )
- add list: InRoom(robot,r<sub>2</sub>), InRoom(o,r<sub>2</sub>)

initial world model, DB<sub>0</sub> (list of ground atoms)

STRIPS problem space = set of operators (with preconds and effects) goal statement (list of atoms)

### desired plan: sequence of ground operators

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262

### **STRIPS Example**

ROOM,

In addition to PushThru, consider

### GoThru $(d, r_1, r_2)$ :

DB<sub>0</sub>:

precondition: InRoom(robot, $r_1$ ), Connects(d, $r_1$ , $r_2$ )

delete list: InRoom(robot,r<sub>1</sub>)

add list: InRoom(robot,r<sub>2</sub>)



**Goal:**  $[Box(x) \land InRoom(x,room_1)]$ 

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### **Progressive planning**

Here is one procedure for planning with a STRIPS like representation: Input : a world model and a goal Output : a plan or fail. ProgPlan[DB,Goal] = If Goal is satisfied in DB, then return empty plan For each operator *o* such that precond(*o*) is satisfied in the current DB: Let DB' = DB + addlist(*o*) – dellist(*o*) Let plan = ProgPlan[DB',Goal] If plan ≠ fail, then return [act(*o*) ; plan] End for

Return fail

This depth-first planner searches forward from the given  $DB_0$  for a sequence of operators that eventually satisfies the goal

DB' is the progressed world state

### **Regressive planning**

Here is another procedure for planning with a STRIPS like representation:

```
Input : a world model and a goal
                                          (ignoring variables)
Output : a plan or fail.
RegrPlan[DB,Goal] =
    If Goal is satisfied in DB, then return empty plan
    For each operator o such that dellist(o) \cap Goal = {}:
         Let Goal' = Goal + precond(o) - addlist(o)
         Let plan = RegrPlan[DB,Goal']
         If plan \neq fail, then return [plan; act(o)]
    End for
    Return fail
```

This depth-first planner searches backward for a sequence of operators that will reduce the goal to something satisfied in DB<sub>o</sub>

Goal' is the regressed goal

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265

### **Computational aspects**

Even without variables, STRIPS planning is NP-hard. Many methods have been proposed to avoid redundant search e.g. partial-order planners, macro operators One approach: application dependent control pick an action Consider this range of GOLOG programs: < any deterministic program > while  $\neg$ Goal do  $\pi a$ . a fully specific about sequence any sequence such that Goal of actions required holds at end easy to execute as hard as planning! In between, the two extremes we can give domain-dependent

guidance to a planner:

while  $\neg$ Goal do  $\pi a$ . [Acceptable(a)?; a]

where Acceptable is formalized separately

This is called forward filtering .

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266

### **Hierarchical planning**

The basic mechanisms of planning so far still preserve all detail needed to solve a problem

- · attention to too much detail can derail a planner to the point of uselessness
- would be better to first search through an abstraction space, where unimportant details were suppressed
- when solution in abstraction space is found, account for remaining details

### ABSTRIPS

precondition wffs in abstraction space will have fewer literals than those in ground space

### e.g., PushThru operator

- high abstraction: applicable whenever an object is pushable and a door exists
- lower: robot and obj in same room, connected by a door to target room
- lower: door must be open
- original rep: robot next to box, near door

predetermined partial order of predicates with "criticality" level

**Reactive systems** 

Some suggest that explicit, symbolic production of formal plans is something to be avoided (especially considering computational complexity)

even propositional case is intractable; first-order case is undecidable

Just "react": observe conditions in the world and decide (or look up) what to do next

can be more robust in face of unexpected changes in the environment

⇒ reactive systems

"Universal plans": large lookup table (or boolean circuit) that tells you exactly what to do based on current conditions in the world

Reactive systems have impressive performance on certain lowlevel problems (e.g. learning to walk), and can even look "intelligent"

but what are the limitations? ...